## Quiz-1 Math of Network Algo. (16 ${ }^{\text {th }}$ Aug 2023)

## Name:

Enroll. Nr.

1. ( 4pt) Describe the following terms: (i) Perceptron, (ii) Activation function, (iii) Neural Network, and (iv) Loss Function.
2. ( 6 pt$)$ Consider a function $\mathrm{f}: \mathbb{R}^{2} \mapsto \mathbb{R}^{2}$ defined as $\mathrm{f}\left(\left(\mathrm{x}_{1}, \mathrm{x}_{2}\right)\right)=\left(-2 \mathrm{x}_{2},-3 \mathrm{x}_{1}+\mathrm{x}_{2}\right)$. Describe geometrical interpretation of the above function in terms translation matrix, mention how a random point is shifted, and special points that may be only stretched.
3. (5pt) Consider a $n \times n$ matrix $A$. Prove that $\|A\|_{F}^{2}=\operatorname{Tr}\left(A \cdot A^{\top}\right)$
4. ( 4 pt ) We flip a fair coin ten times. Find the probability of the following events: (i) Nr of heads and talks are equal. (ii) Nr of heads is more than nr of tails. (iii) The $\mathfrak{i}^{\text {th }}$ flip and $(11-\mathfrak{i})^{\text {th }}$ flip are same for every $\mathfrak{i} \in[5]$.
5. ( 6 pt ) We roll two fair dice. What is the probability space? What is the expectation of random variable representing the sum of two dice?
6. (5pt) Write steps in Principal Component Analysis to reduce 2-dimension data to 1-dimension data.
