Quiz 0: MT3164: Numerical Analysis

11:00 am to 11:50 am on 13^{th} August, 2025

This quiz contains series of tasks. Please complete all of them. Do not leave the lab before you got confirmation of your submission.

- 1. Open Visual Studio (or some other editor).
- 2. Create a new file q0p1.py and save it on Desktop.
- 3. A typical question will be of the following format.
 - (a) Write a program that takes as input an integer M and float values a, b, δ, ϵ and computes a 'reasonable' root of the following function in the range [a, b] using the bisection method.

$$f(x) = \frac{x^3 + 4x^2 + 3x + 5}{2x^3 - 9x^2 + 18x - 2}.$$

Output a, b, f(a), f(b) at each stage. We say a root $c \in [a, b]$ is reasonable if one of the following conditions is true: (i) it is obtained after M^{th} iteration of the algorithm, (ii) $|f(c)| < \epsilon$, or (iii) the error between the actual root and c is at most δ .

Input: $M, a, b, \delta, \epsilon$

Output: Your name and roll number in the first line.

Next M lines should contains the following four values a, b, f(a), f(b).

- 4. Before starting to solve the problem, it would be good to obtain sample input size.
 - cp /nfscommon/common/prafullkumar/public/input_q0p1.txt ./
- 5. An ideal program looks as follows.

```
1 def f(x):
      # The given function
      return (x**3 + 4*x**2 + 3*x + 5) / (2*x**3 - 9*x**2 + 18*x - 2)
  def bisection_method(M, a, b, delta, epsilon):
      fa = f(a)
      fb = f(b)
      if fa * fb > 0:
9
          print("No root in the range.")
          return None
11
12
      for i in range (1, M + 1):
13
          print(f"{i:4d} {a:12.4f} {b:12.4f} {fa:12.4e} {fb:12.4e}")
          c = (a + b) / 2
16
          fc = f(c)
17
18
          # Check stopping conditions
19
          if abs(fc) < epsilon or (b - a) / 2 <= delta:</pre>
20
21
```

```
# Update the interval
           if fa * fc < 0:</pre>
25
               fb = fc
26
           else:
27
               a = c
28
               fa = fc
29
30
      # If reached M iterations, return c
31
      c = (a + b) / 2
      return c
33
34
36 M = int(input())
a = float(input())
38 b = float(input())
39 delta = float(input())
40 epsilon = float(input())
42 print("20001 \t Alan Turing")
43 # Replace 20001 by your roll number and 'Alan Turing' by your name.
44 bisection_method(M, a, b, delta, epsilon)
```

6. Check the output of your program using the following command.

```
python3 q0p1.py < input_q0p1.txt</pre>
```

Make sure that all these files are on your Desktop.

7. Submit the solutions only if you are confident with it. You can submit a solution only once. Use the following command for submission.

```
/nfscommon/common/prafullkumar/submit q0p1.py
```

- 8. Please confirm with the instruction whether your submission is successful or not.
- 9. Use the following command to change your default password.

passwd